PHYSICS FORMULAS

Electron = $-1.602 \ 19 \times 10^{-19} \ C$ = $9.11 \times 10^{-31} \ kg$ Proton = $1.602 \ 19 \times 10^{-19} \ C$ = $1.67 \times 10^{-27} \ kg$ Neutron = $0 \ C$ = $1.67 \times 10^{-27} \ kg$

 6.022×10^{23} atoms in one atomic mass unit

e is the elementary charge: 1.602 19 × 10⁻¹⁹ C Potential Energy, velocity of electron: $\mathbf{P} = eV = \frac{1}{2}$

Quadratic (Watts W)

Quadratic (Watts W)

Kinetic Ener

Equation: 2a

 $\frac{2a}{2a} = \frac{1}{2}mv$

[Natural Log: when $e^b = x$, $\ln x = b$] m: 10^{-3} µ: 1^{-6} n: 10^{-9} p: 10^{-15} a: 10^{-18}

Addition of Multiple Vectors:

$$\begin{split} \vec{R} &= x + \beta + \vec{C} & \text{Resultant} = \text{Sum} \\ \vec{R}_x &= \vec{A}_x + \vec{B}_x + \vec{C}_x & x\text{-component} \\ \vec{R} &= \vec{l}_y + \vec{B}_y + \vec{l}_y & y\text{-component} \\ R &= \sqrt{R_x^2 + R_y^2} & \text{Magnitude (leng)} \\ \theta_R &= \tan^{-1} \frac{R_y}{R_x} & \text{or} & \tan \theta_R = \frac{R_y}{R_x} & \text{Angle of} \end{split}$$

Multiplication of Vectors:

Cross Product or Vector Product:

$$i \times j = k$$
 $j \times i = -k$
 $i \times i = 0$

Dot Product or Scalar Product:

$$i \cdot j = 0$$
 $i \cdot i = 1$
 $\mathbf{a} \cdot \mathbf{b} = ab \cos \theta$



Positive direction:

Derivative of Vectors:

Velocity is the derivative of position with respect to time:

$$\mathbf{v} = \frac{d}{dt}(x\mathbf{i} + y\mathbf{j} + z\mathbf{k}) = \frac{dx}{dt}\mathbf{i} + \frac{dy}{dt}\mathbf{j} + \frac{dz}{dt}\mathbf{k}$$

Acceleration is the derivative of velocity with respect to time:

$$\mathbf{a} = \frac{d}{dt}(v_x \mathbf{i} + v_y \mathbf{j} + v_z \mathbf{k}) = \frac{dv_x}{dt} \mathbf{i} + \frac{dv_y}{dt} \mathbf{j} + \frac{dv_z}{dt} \mathbf{k}$$

Rectangular Notation: $Z=R\pm jX$ where +j represents inductive reactance and -j represents capacitive reactance. For example, $Z=8+j6\Omega$ means that a resistor of 8Ω is in series with an inductive reactance of 6Ω .

Polar Notation: $Z = M \angle \theta$, where M is the magnitude of the reactance, and θ is the direction with respect to the horizontal pure resistance) axis. For example, a resistor of 4Ω in sec., with a capacitor with a reactance of 3Ω would be expressed as $5 \angle 3 = 3^{\circ} \Omega$.

 4Ω in sec. with a capacitor with a reactance of 3Ω would be expressed as $5 \angle -2.00^\circ \Omega$. In the descriptions above impedance is used as an example. Rectangular and Fular Notation can also be used to express amperage, voltage, and power.

To content from rectangular to lar notation:

GIVE : X - jY (care with the sign before the "j")

Magnitude: $\sqrt{X^2 + Y^2} = M$

Angle: $\tan\theta = \frac{-Y}{X} \qquad \begin{array}{l} \text{(negative sign carried over} \\ \text{from rectangular notation} \\ \text{in this example)} \end{array}$

St add 180° af a taking the inverse tangent. If the greater than 180°, you may optionally subtract tain the value posest to the relative angle.

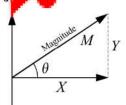
nvert from polar to rectargular (j) detion

e: $M \angle \theta$ $M \cos \theta$ Alue: $M \sin \theta$

In conversions, the j value will have the same sign as the θ value for angles having a magnitude < 180°.

Use rectangular notation when adding and subtracting.

Use polar notation for multiplication and division. Multiply in polar notation by multiplying the magnitudes and adding the angles. Divide in polar notation by dividing the magnitudes and subtracting the denominator angle from the numerator angle.





ELECTRIC CHARGES AND FIELDS

Coulomb's Law: [Newtons M]

$$F = k \frac{|q_1||q_2|}{r^2} \qquad \text{where:} \qquad F = \text{force on one charge by} \\ \qquad \qquad \text{the other}[N] \\ \qquad \qquad k = 8.99 \times 10^9 \ [\text{N} \cdot \text{m}^2/\text{C}^2] \\ \qquad \qquad \qquad q_1 = \text{charge } [C] \\ \qquad \qquad \qquad q_2 = \text{charge } [C]$$

Electric Field: [Newtons/Coulomb or Volts/Meter]

$$E = k \frac{|q|}{r^2} = \frac{|F|}{|q|} \qquad \text{where:} \qquad E = \text{electric old N/C or } m$$

$$k = 8.0 \times 10 \quad \text{N} \cdot \text{m}^2/\text{C}^2$$

$$q = \text{change [C]}$$

$$r = \text{stance } [m]$$
force

r = distance [m]

Electric field lines radiate outward from positive c The electric is zero incide a conductor.

Relationship

$$k = \frac{1}{4\pi \in \mathbb{R}} \quad \text{where:} \quad k = 0.3 \times 10^9 \, [\text{N·m}^2/\text{C}^2]$$

$$= \text{permittivity of free s}$$

$$8.85 \times 1$$

Electric Field due Infinite Line of

$$E = -\frac{\lambda}{t} \stackrel{?}{\in_0} r = \frac{2k\lambda}{r} \stackrel{E}{=} \begin{array}{l} E = \text{electric field [N/C]} \\ \lambda = \text{charge r} \\ \varepsilon_0 = \text{permitti.} \\ 8.85 \times 1 \\ r = \text{distance } [m] \\ k = 8.99 \times 10^9 [\text{N} \cdot \text{m}^2] \end{array}$$

Electric Field due to ring of Charge: [N/C]

$$E = \frac{kqz}{\left(z^2 + R^2\right)^{3/2}}$$

$$E = \text{electric field [N/C]}$$

$$k = 8.99 \times 10^9 [\text{N·m²/C²}]$$

$$q = \text{charge [C]}$$

$$z = \text{distance to the charge [m]}$$

$$R = \text{radius of the ring [m]}$$

Electric Field due to a disk Charge: [N/C]

$$E = \frac{\sigma}{2 \in_{0}} \left(1 - \frac{z}{\sqrt{z^{2} + R^{2}}}\right) \quad \begin{array}{l} E = \text{electric field [N/C]} \\ \sigma = \text{charge per unit area} \\ \text{[C/m}^{2}\} \\ \in_{0} = 8.85 \times 10^{-12} \text{ [C}^{2}/\text{N} \cdot \text{m}^{2}]} \\ z = \text{distance to charge [m]} \\ R = \text{radius of the ring [m]} \end{array}$$

Electric Field due to an infinite sheet: [N/C]

$$E = \frac{\sigma}{2 \in_{0}} \qquad \begin{aligned} E &= \text{ electric field } [\textit{N/C}] \\ \sigma &= \text{ charge per unit area } [\textit{C/m}^{2}\} \\ \in_{0} &= 8.85 \times 10^{-12} \ [\textrm{C}^{2}/\textrm{N}\cdot\textrm{m}^{2}] \end{aligned}$$

Electric Field inside a spherical shell: [N/C]

$$E = \frac{kqr}{R^3} \hspace{1cm} E = \text{electric field [N/C]} \\ q = \text{charge [C]} \\ r = \text{distance from center of sphere to} \\ \text{the charge [m]} \\ R = \text{radius of the sphere [m]}$$

Electric Field outside a spherical shell: [N/C]

$$E = \frac{kq}{r^2}$$

$$E = \text{electric field [N/C]}$$

$$q = \text{charge [C]}$$

$$r = \text{distance from center of sphere to}$$

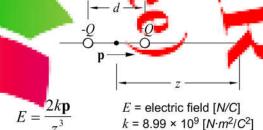
$$\text{the charge [m]}$$

wer per unit area of an electric or verage magne

$$W/m^2 = rac{E_m^2}{2\mu_0 c} = rac{B_n^2}{2\mu_0}$$
 $W = \text{watts}$ $h = \text{max. electric field [N/C]}$ $\mu_0 = 4\pi \times 10^{-7}$ $c = 1.99792 \times 10^8 \text{ [m/s]}$ $B_m = \text{max. magnetic field [7]}$

e moving in the same direction as the electric A positive diag field direction losses potential energy in the potential of the electric field direction lishes in this arrection.

tric Dipole: 🌠 charges of equa magnitude and ite polarity separated by a distan



$$E = \frac{1}{z^3}$$

$$k = 8.99 \times 10^9 \ [N \cdot m^2/C^2]$$

$$\epsilon_0 = \text{permittivity of free space } 8.85 \times 10^{-12} \ C^2/N \cdot m^2$$

$$\mathbf{p} = qd \ [C \cdot m] \text{ "electric dipole moment" in the direction negative to positive}$$

$$z = \text{distance [m] from the dipole center to the point along the dipole axis where the electric field}$$

is to be measured

Deflection of a Particle in an Electric Field:

$$2 ymv^2 = qEL^2$$
 $y = deflection [m]$
 $m = mass of the particle [kg]$
 $d = plate separation [m]$
 $v = speed [m/s]$
 $q = charge [C]$
 $E = electric field [N/C or V/m]$
 $L = length of plates [m]$



Potential Difference between two Points: [volts V]

$$\Delta V = V_B - V_A = \frac{\Delta PE}{q} = -Ed$$

 ΔPE = work to move a charge from A to B [N·m or J]

q = charge [C]

 $V_{\rm B}$ = potential at B [V]

 V_A = potential at A [V]

E = electric field [N/C or V/m

d = plate separation [m]

Electric Potential due to a Point Charge: [volts V]

$$V = k \frac{q}{r}$$

V = potential [volts V]

 $k = 8.99 \times 10^9 [N_{\rm m}^2/{\rm d}^2]$

q = charge[C]

r = distan[m]

Potential Energy of a Pair of Charges: [J, N·m or

$$PE = q_2 V_1 = k \frac{q_1 q_2}{q_2}$$

Valis the electric potential d

 q_2V_1 is the orkerequired to q2 from init

Work and P

$$\Delta U = U_I - W$$

$$U = -W$$

$$W = \mathbf{r} \cdot \mathbf{d} = Fd \operatorname{co}^{\mathbf{Q}}$$

$$W = a \mathbf{r} \cdot d\mathbf{s}$$

$$\Delta V = V_f - V_i = -\frac{r}{q}$$

$$V = -\int_{i}^{f} \mathbf{E} \cdot d\mathbf{s}$$

U electric potential energ

= work done on a par a field [J]

 W_{∞} = work don brought f potential) to location [J]

F = is the

 $\mathbf{d} = \mathbf{is} \text{ the } \mathbf{d}_{\mathbf{k}}$ which the applied[m]

F =is the force sca

d = is the distance

 θ = is the angle between the force and distance vectors

ds = differential displacement of the charge [m]

V = volts[V]

q = charge [C]

Flux: the rate of flow (of an electric field) $[N \cdot m^2/C]$

$$\Phi = \oint \mathbf{E} \cdot d\mathbf{A}$$

$$= \int E(\cos\theta) dA$$

 Φ is the rate of flow of an electric field [N·m²/C]

integral over a closed surface

E is the electric field vector [N/C] A is the area vector $[m^2]$ pointing outward normal to the surface.

Gauss' Law:

$$\in_{\scriptscriptstyle{0}} \Phi = q_{\scriptscriptstyle{enc}}$$

$$\in_0 \oint \mathbf{E} \cdot d\mathbf{A} = q_{enc}$$

 $\epsilon_0 = 8.85 \times 10^{-12} [C^2/N \cdot m^2]$

Φ is the rate of flow of an electric field $[N \cdot m^2/C]$

 q_{enc} = charge within the gaussian surface [C]

integral over a closed surface

E is the electric field vector [J]

A is the area vector [m2] pointing outward normal to the surface.

CAPACITANCE

Parallel-Capacit

$$G = \kappa \in_0 \frac{A}{d}$$

capacitance [farads F]

= the dielectric constant (1)

 ϵ_0 = permittive of free space 8.95 × 12 $C^2/N \cdot m^2$

 $A = \text{area of the plate } [m^2]$

d = separation below plates [m]

dindrical Capa

$$C = 2\pi\kappa \in_{0} \frac{1}{\ln(b)}$$

C = capacitan [farads F]

κ = dielectionstant (1)

 $\epsilon_0 = 8.85 \cdot 10^{-12} \ C^2/N \cdot m^2$ L = length [m]

b = radius

conductor 4

radius of ie conductor [m]

Capacitor:

$$C = 4\pi\kappa \in_{0} \frac{ab}{b-a}$$

C = capacitance [farads F]

 κ = dielectric constant (1)

 $\epsilon_0 = 8.85 \times 10^{-12} \ C^2/N \cdot m^2$ b = radius, outer conductor

a = radius, inner conductor [m]

Maximum Charge on a Capacitor: [Coulombs C]

$$Q = VC$$

Q = Coulombs [C]

V = volts[V]

C = capacitance in farads [F]

For capacitors connected in series, the charge Q is equal for each capacitor as well as for the total equivalent. If the dielectric constant κ is changed, the capacitance is multiplied by κ , the voltage is divided by κ , and Q is unchanged. In a vacuum $\kappa = 1$, When dielectrics are used, replace \in_0 with $\kappa \in_0$.

Electrical Energy Stored in a Capacitor: [Joules J]

$$U_E = \frac{QV}{2}$$



Charge per unit Area: [C/m²]

$$\sigma = \frac{q}{A}$$

$$\sigma = \text{charge per unit area } [C/m^2]$$

$$q = \text{charge } [C]$$

$$A = \text{area } [m^2]$$

Energy Density: (in a vacuum) [J/m³]

$$u = \frac{1}{2} \in_{0} E^{2}$$
 $u = \text{energy per unit volume } [J/m^{3}]$
 $\in_{0} = \text{permittivity of free space}$
 $8.85 \times 10^{-12} C^{2}/N \cdot m^{2}$
 $E = \text{energy } [J]$

Capacitors in Series:

$$\frac{1}{C_{\it eff}} = \frac{1}{C_1} + \frac{1}{C_2} \, \dots$$

$$C_{eff} C_1 C_2 \dots$$

Capacitors connected in series all have the same ch For parallel to the sum of charge on each capacitor.

Time Constant [seconds]

$$\tau = RC$$

$$\tau = \text{time it takes the capacitor to reach } 60^{\circ}$$
of its maximum charge [seconds]
$$R = \text{series relatance [ohms Ol}$$

$$C = \text{capacitance [farads } F]$$

Charge or Voltage fter ? Seconds:

charging:
$$q$$
 = charge after t so [coulombs C]
$$q + Q(1 - e^{-t} - t) \qquad Q = \text{maxim} \qquad \text{Lombs}$$

$$= L_3(1 - e^{-t/\tau}) \qquad e = \text{natural log}$$

 V_S = supply volts V

discharging:
$$t = \text{time [seconds]}$$
 $q = Qe^{-t/\tau}$ $\tau = \text{time constant } RO$
 $V = \text{volts [V]}$
 $V = V_S e^{-t/\tau}$ $V = \text{supply volts [V]}$

[Natural Log: when $e^b = x$, $\ln x = b$]

Drift Speed:

$$I = \frac{\Delta Q}{\Delta t} = \left(nqv_d A \right) \qquad \begin{array}{l} \Delta Q = \text{\# of carriers} \times \text{charge/carrier} \\ \Delta t = \text{time in seconds} \\ n = \text{\# of carriers} \\ q = \text{charge on each carrier} \\ v_d = \text{drift speed in meters/second} \\ A = \text{cross-sectional area in meters}^2 \end{array}$$

RESISTANCE

Emf: A voltage source which can provide continuous current [volts]

$$\epsilon = IR + Ir$$
 ϵ = emf open-circuit voltage of the battery I = current [amps] R = load resistance [ohms] r = internal battery resistance [ohms]

Resistivity: [Ohm Meters]

$$\rho = \frac{E}{J} \qquad \qquad \rho = \text{resistivity } [\Omega \cdot m] \\ E = \text{electric field } [N/C] \\ \rho = \frac{RA}{L} \qquad \qquad J = \text{current density } [A/m^2] \\ R = \text{resistance } [\Omega \text{ ohms}] \\ A = \text{area } [m^2] \\ L = \text{length of conductor } [m]$$

Variation of Resistance with Temperature:

$$\rho-\rho_0=\rho_0\alpha(T-T_0) \qquad \rho=\text{resistivity } [\Omega\cdot m] \\ \rho_0=\text{reference resistivity } [\Omega\cdot m] \\ \alpha=\text{temperature coefficient of resistivity } [K^1] \\ T_0=\text{reference temperature} \\ T-T_0=\text{temperature difference} \\ [K \text{ or } ^\circ C]$$

CURREN

Current D

Current Der It:
$$[A/m^2]$$
 $i = \int \mathbf{J} \cdot d\mathbf{A}$

It is uniform rallel to $d\mathbf{A}$, $i = JA$
 i

f Change of Chemical Energy

P = power[W]i = current [A] ε = emf potential [V]

Kirchhoff's Rules

- The sum of the currents entering a junctions is equal to the sum of the currents leaving the junction.
- The sum of the potential differences across all the elements around a closed loop must be zero.

Evaluating Circuits Using Kirchhoff's Rules

- Assign current variables and direction of flow to all branches of the circuit. If your choice of direction is incorrect, the result will be a negative number. Derive equation(s) for these currents based on the rule that currents entering a junction equal currents exiting the junction.
- Apply Kirchhoff's loop rule in creating equations for different current paths in the circuit. For a current path beginning and ending at the same point, the sum of voltage drops/gains is zero. When evaluating a loop in the direction of current flow, resistances will cause drops (negati

they wi The nu



MAGNETISM

André-Marie **Ampére** is credited with the discovery of electromagnetism, the relationship between electric currents and magnetic fields.

Heinrich **Hertz** was the first to generate and detect electromagnetic waves in the laboratory.

Magnetic Force acting on a charge q: [Newtons N]

 $F = qvB\sin\theta$ F = force [N] q = charge [C] v = vel city [n] p = magnetic field [T] p = magnetic field [T] p = magnetic field [T]

Right-Hand Rule: Fingers present the direction of the magnetic force B, thumb represents the direction of at any angle to B), and the force F on a **positive** have emanates from palm. The direction of a magnetic field is from **north to south**. Use the left hand for a negative charge.

Also, if a wire to grasped in the tight band with the thum in the on the part of current flow the fingers will curl the direction of the magnetic field.

In a solenoid with current flowing in the financial magnetic field is in the direct

first magnetic field is in the direct
When applied to a strical flow caused
magnetic field, things get more complicate
north pole of a magnet moving toward a look
(magnetic field increasing). The the ents the lo. However electrical activity the change in the magnetic field, so that actually flow in the opposite direction. If the being withdrawn, then the suggested currer decreasing so that the actual current flowin th direction of the fingers in this case to oppose the decrease. Now consider a cylindrical area of magnetic field going into a page. With the thumb pointing into the page, this would suggest an electric field orbiting in a clockwise direction. If the magnetic field was increasing, the actual electric field would be CCW in opposition to the increase. An electron in the field would travel opposite the field direction (CW) and would experience a negative change in potential.

Force on a Wire in a Magnetic Field: [Newtons N]

 $F = BI \ \ell \sin \theta \qquad \qquad F = \text{force } [N] \\ B = \text{magnetic field } [T] \\ F = I \ \ell \times B \qquad \qquad I = \text{amperage } [A] \\ \ell = \text{length } [m] \\ \theta = \text{angle between } B \text{ and the direction of the current}$

Torque on a Rectangular Loop: [Newton meters N·m]

 $\tau = NBIA \sin \theta$ N = number of turns B = magnetic field [T] I = amperage [A] $A = \text{area } [m^2]$ $\theta = \text{angle between } B \text{ and the plane of the loop}$

Charged Particle in a Magnetic Field:

 $r = \frac{mv}{qB}$ r = radius of rotational path m = mass [kg] v = velocity [m/s] q = charge [C] p = magnetic field [T]

Magnetic Field Around a Wire: [T]

 $B = \frac{\mu_0 I}{2\pi r}$ B = magnetic field [7] $\mu_0 = \text{the permeability of free}$ $\text{space } 4\pi \times 10^{-7} \text{ T·m/A}$ I = current [A] r = distance from the center ofthe conductor

Magnetic at the center of an Arc: [T]

 $B = \frac{\mu_0 i \phi}{4\pi r}$ B = magnetic field [T] $\mu_0 = \text{the permeability of free space } 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$ i = current [A] $\phi = \text{the rec in radians}$ r = distrace from the center of the conductor

Hall Effect: Voltage across the width of a magnetic Field:

etween Two Conductors: The force is ive if the currents are in the same direction.

 $\frac{F_1}{\ell} = \frac{\mu_0 I_1 I_2}{2\pi d}$ F = force [N] $\ell = \text{length } [m]$ $\mu_0 = \text{the permeability of free space } 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$ I = current [A] d = distance center to center [m]

Magnetic Field Inside of a Solenoid: [Teslas 7]

B = magnetic field [T] $\mu_0 = \text{the permeability of free}$ $\text{space } 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$ n = number of turns of wire per unit length [#/m] I = current [A]

Magnetic Dipole Moment: [J/T]

 $\mu = NiA \qquad \begin{array}{l} \mu = \text{the magnetic dipole moment } [J/T] \\ N = \text{number of turns of wire} \\ i = \text{current } [A] \\ A = \text{area } [m^2] \end{array}$

Magnetic Flux through a closed loop: [T·M² or Webers]



Magnetic Flux for a changing magnetic field: $[T \cdot M^2]$ or Webers

$$\Phi = \int \mathbf{B} \cdot d\mathbf{A}$$

$$B = \text{magnetic field } [T]$$

$$A = \text{area of loop } [m^2]$$

A Cylindrical Changing Magnetic Field

$$\oint \mathbf{E} \cdot d\mathbf{s} = E2\pi \, r = \frac{d\Phi_B}{dt} \qquad \begin{array}{l} E = \text{electric field [N/C]} \\ r = \text{radius [m]} \\ t = \text{time [s]} \\ \Phi = BA = B\pi \, r^2 \qquad \qquad \Phi = \text{magnetic flux [T\cdot m^2 or Webers]} \\ B = \text{magnetid field [interpretation of the magnetic field [interpretation o$$

Faraday's Law or Induction stees that the instantaneous and induced in a circuit equals the rate of change of gnetic flux through the circuit. Michael Fara made fund mental discoveries in magnetism electricity, and light.

$$\Delta \Phi$$
 $\Delta \Phi$ N number of Δt Φ = magnetic f Δt = time [s]

Lenz's Law states that the polarity of the index on its such that it produces a current who can exict field on oses the change in magnetic curt

Motional emf is induced when a conducing batteries through a perpendicular magnetic field.

$$\varepsilon = B\ell v$$
 $\theta = \text{magnetic field}$ $\ell = \text{length of the}$ $v = \text{speed of the bar } [m/s]$

emf Induced in a Rotating Coil:

$$\varepsilon = NAB\omega \sin \omega t \qquad \begin{array}{l} N = \text{number of turns} \\ A = \text{area of loop } [m^2] \\ B = \text{magnetic field } [T] \\ \omega = \text{angular velocity } [rad/s] \\ t = \text{time } [s] \end{array}$$

Self-Induced emf in a Coil due to changing current:

$$\varepsilon = -L \frac{\Delta I}{\Delta t} \qquad \begin{array}{c} L = \text{ inductance } [H] \\ I = \text{ current } [A] \\ t = \text{ time } [s] \end{array}$$

Inductance per unit length near the center of a solenoid:

$$\frac{L}{\ell} = \mu_0 n^2 A$$

$$L = \text{inductance } [H]$$

$$\ell = \text{length of the solenoid } [m]$$

$$\mu_0 = \text{the permeability of free space}$$

$$4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$$

$$n = \text{number of turns of wire per unit}$$

$$\text{length } [\#/m]$$

$$A = \text{area } [m^2]$$

Amperes' Law:

$$\oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 i_{enc}$$

$$B = \text{magnetic field [T]}$$

$$\mu_0 = \text{the permeability of free space}$$

$$4\pi \times 10^{-7} \text{ T·m/A}$$

$$i_{enc} = \text{current encircled by the}$$

$$\log |A|$$

Joseph Henry, American physicist, made improvements to the electromagnet.

James Clerk **Maxwell** provided a theory showing the close relationship between electric and magnetic phenomena and predicted that electric and magnetic fields could move through space as waves.

J. **Thomson** is credited with the discovery of the electron 1897.

INDUCTIFE & REL CIRCUITS

Induana of a Coil: [H]

$$L = \frac{N}{L}$$
 $N = \text{number of turns}$
 $\Phi = \text{number of flux } [T \cdot m^2]$
 $I = \text{current } [L]$

In an RL Circuit, over one time constant $(\tau = L/R)$ the rent in the circuit is 3.2% of its final value, ε/R .

Circuit:

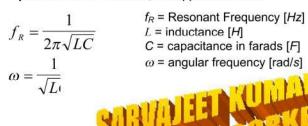
Magnetic Energy Stored in an Inductor:

$$U_{B}=\frac{1}{2}LI^{2}$$
 $U_{B}=$ Potential Energy [J] $L=$ inductance [H] $I=$ current [A]

Electrical Energy Stored in a Capacitor: [Joules J]

$$U_E = \frac{QV}{2} = \frac{CV^2}{2} = \frac{Q^2}{2C} \quad \begin{array}{ll} U_E = \text{Potential Energy [J]} \\ Q = \text{Coulombs [C]} \\ V = \text{volts [V]} \\ C = \text{capacitance in farads [F]} \end{array}$$

Resonant Frequency: The frequency at which $X_L = X_C$. In a **series**-resonant circuit, the impedance is at its minimum and the current is at its maximum. For a **parallel**-resonant circuit, the opposite is true.



Voltage, series circuits: [V]

 $V_C = \frac{q}{C}$ $V_R = IR$ $V_{\rm C}$ = voltage across capacitor [V] q = charge on capacitor [C] f_R = Resonant Frequency [Hz] $\frac{V_X}{X} = \frac{V_R}{R} = I$ $\frac{I_R - \text{Resolitant Field}}{L = \text{inductance } [H]}$ C = capacitance inC = capacitance in farads [F] $V^2 = V_p^2 + V_v^2$ R = resistance [Ω] I = current [A]

> V = supply voltage [V] $V_{\rm X}$ = voltage across reactance [V] V_R = voltage across resistor [V]

Phase Angle of a series RL or RC circuit. [de

$$\tan \phi = \frac{X}{R} = \frac{V_X}{V_R} \qquad \qquad \phi = \text{Phase angle [a grees]}$$

$$X = \text{reactan a } [\Omega]$$

$$Z = \text{resistanc.} [\Omega]$$

$$Z = \text{resistanc.} [\Omega]$$

$$V_X = \text{voltage across reactanc.} [V]$$

$$V_X = \text{voltage across resistor.} [V]$$

$$V_X = \text{voltage across resistor.} [V]$$

$$Z = \text{impedative.} [V]$$

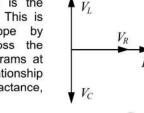
Impedance f a series RL or Re cleat: [Ω]

$$Z^2 = R^2 + A$$
 $\varphi = \text{Phase Angle [degrees]}$ $E = IZ$ $\varphi = \text{Phase Angle [degrees]}$ $\varphi =$

Serie RCL Circuits:

The Reschant Phasor
$$Y = X_L - X_C$$
 is in the direction of the larger reactance and determines whether the circuit is inductive or capacitive. If X_L is larger than X_C , then the circuit is inductive and X is a vector in the upward direction.

In series circuits, the amperage is the reference (horizontal) vector. This is observed on the oscilloscope by looking at the voltage across the resistor. The two vector diagrams at right illustrate the phase relationship between voltage, resistance, reactance, and amperage.



 X_C

$$Z^{2} = R^{2} + (X_{L} - X_{C})^{2}$$
 $Z = \frac{R}{\cos \phi}$

Impedance may be found by adding the components using vector algebra. By converting the result to polar notation, the phase angle is also found.

For multielement circuits, total each resistance and reactance before using the above formula.

Damped Oscillations in an RCL Series Circuit:

$$q = Qe^{-Rt/2L}\cos(\omega't + \phi)$$

$$\omega' = \sqrt{\omega^2 - (R/2L)^2}$$

$$\omega = 1/\sqrt{LC}$$

When R is small and $\omega' \approx \omega$:

$$=\frac{Q^2}{2C}e^{-Rt/L}$$

q = charge on capacitor [C]

Q = maximum charge [C]

e = natural log

 $R = \text{resistance } [\Omega]$

L = inductance [H]

 ω = angular frequency of the undamped oscillations [rad/s]

 ω = angular frequency of the damped oscillations [rad/s]

U = Potential Energy of the capacitor [J]

C = capacitance in farads [F]

Parallel RCL



total current and mase angle in <u>multiplement circuits</u>, and *I* for each path and add vectorally. Note that when proverting between current and resistance, a division will be requiring the use of polar notation and resulting e of sign for the engle since it will be divided into aced from) an angle of zero.

valent Series Circuit: Given the Z in part Acircuit, the resistance and actuace of the ent series circuit is as follows:

$$R = Z_T \cos \theta \qquad \qquad X = Z_T \sin \theta$$

AC CIRCUITS

Instantaneous Voltage of a Sine Wave:

$$V = V_{\text{max}} \sin 2\pi f t$$
 $V = \text{voltage } [V]$ $f = \text{frequency } [H_z]$ $t = \text{time } [s]$

Maximum and rms Values:

$$I = \frac{I_m}{\sqrt{2}}$$
 $V = \frac{V_m}{\sqrt{2}}$ $I = \text{current } [A]$ $V = \text{voltage } [V]$

RLC Circuits:

tan
$$\phi = \frac{X_L - X_C}{R}$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

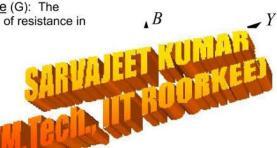
$$P_{avg} = IV \cos \phi$$

$$PF = \cos \phi$$

Conductance (G): The reciprocal of resistance in siemens

Susceptan reciproc siemens Admittanc

of imper



ELECTROMAGNETICS

| | WAVELENGTH |
|--|--|
| $c = \lambda f$ $c = E / B$ $1 \text{Å} = 10^{-10} \text{m}$ | c = speed of light 2.998 × 10 ⁸ m/s λ = wavelength [m] f = frequency [Hz] E = electric field [N/C] B = magnetic field [T] \mathring{A} = (angstrom) unit of wavelength equal to 10 ⁻¹⁰ m m = (meters) |

WAVELENGTH SPITTER

| BAND | METERS | NGSTROMS |
|--------------------|---------------|------------------------------------|
| Longwave radio | 1 100 km | $10^{13} - 10^{15}$ |
| Standard Broadcast | 100 - 1000 m | 10 ¹² - 10 |
| Shortwave radio | 10 100 m | 10 ¹¹ - 10 ¹ |
| TV, FM | -0.1 - 10 m | 10° •10 ¹¹ |
| Microwaye | 1 - 100 mi | 10 ⁷ - 10 ⁹ |
| Infrared | 0.8 - 1 00 µm | 8000 - 10 ⁷ |
| Visible light | 360 690 nm | 3600 - |
| violet | 360 nm | |
| blue | 130 nm | |
| green 🖊 | 490 nm | 4900 |
| ye w | -560 nm 🔫 | |
| ange | 600 nm | |
| red | 690 nm | 690 |
| Ultraviolet light | 10 - 390 nm | 1 |
| X-rays | 5 - 10,000 pm | 0.05 - 100 |
| Gamma rays | 100 - 5000 fm | 0.001 - 0.05 |
| Cosmic rays | < 100 fm | < 0.001 |

Intensity of Electromagnetic Radiation [watts/m²]:

$$I = \frac{P_s}{4\pi r^2}$$
 $I = \text{intensity } [w/m^2]$
 $P_s = \text{power of source } [\text{watts}]$
 $r = \text{distance } [m]$
 $4\pi r^2 = \text{surface area of sphere}$

Force and Radiation Pressure on an object:

| a) if the light is totally | 1 |
|--|---|
| absorbed: | |

$$F = \frac{IA}{c} \qquad P_r = \frac{I}{c}$$

b) if the light is totally reflected back along the path:

$$F = \frac{2IA}{c} \qquad P_r = \frac{2I}{c}$$

+*ni* – 3diiac

ure on an object

F = force [N] $I = \text{intensity } [w/m^2]$

 $A = area [m^2]$

 P_r = radiation pressure [N/m²]

 $c = 2.99792 \times 10^8 [m/s]$

Poynting Vector [watts/m²]:

$$S = \frac{1}{\mu_0}EB = \frac{1}{\mu_0}E^2$$

$$E = \frac{1}{\mu_0}EB = \frac{1}{\mu_0}E^2$$

$$E = \text{electric field } [N/C \text{ or } V/M]$$

$$E = \text{magnetic field } [T]$$

$$CB = E$$

$$C = 2.99792 \times 10^8 \text{ } [m/s]$$

LIGHT

| Indices of Refraction: | Quartz: | 1.458 |
|------------------------|--------------|-----------|
| 7 | Glass, crown | 1.52 |
| 1 | Glass, flint | 1.66 |
| | Water | 1.333 |
| | Air | 1.000 293 |

Angle of inchence The angle measured from the perpendicular to the ace or from the perpendicular to the tan ent to the face

Inder Refraction: Materials greater density have a higher index of refraction.

$$n \equiv \frac{c}{v}$$
 = index of refraction
= speed of light in the actium 3×10^8 m/s
= speed of light in the material [m/s]

$$\frac{\lambda_0}{\lambda_n} = v_0 \text{ velength of the light in a vacuum } [m]$$

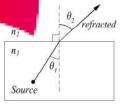
$$\lambda_v = \text{if wavelength in the laterial } [m]$$

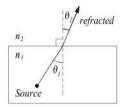
fraction: Selles Law



traveling to a region of density: $\theta_2 > \theta_1$

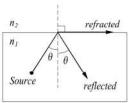
traveling to region of greater density: $\theta_2 < \theta_1$





<u>Critical Angle</u>: The maximum angle of incidence for which light can move from n_1 to n_2

$$\sin \theta_c = \frac{n_2}{n_1} \qquad \text{for } n_1 > n_2$$



Sign Conventions: When M is

negative, the image is inverted. p is positive when the object is in front of the mirror, surface, or lens. Q is positive when the image is in front of the mirror or in back of the surface or lens. f and r are positive if the center of curvature is in front of the mirror or in back of the surface or lens.

Magnification by spherical mirror or thin lens. A





Plane Refracting Surface:

plane refracting surface:

$$\frac{n_1}{p} = -\frac{n_2}{i}$$

p = object distance i = image distance [m]n = index of refraction

Lensmaker's Equation for a thin lens in air:

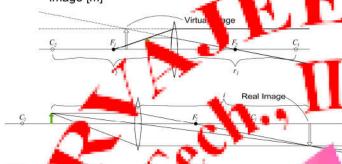
$$\frac{1}{f} = \frac{1}{p} + \frac{1}{i} = (n-1)\left(\frac{1}{r_1} - \frac{1}{r_2}\right)$$

f = focal length [m]i = image distance [m]p = object distance [m]

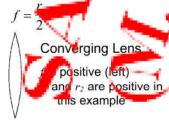
n = index of refraction

 r_1 = radius of surface nearest the object[m]

 r_2 = radius of surface nearest the image [m]



Thin Lens n the thick st parts thin compared i is negative on the left, pose on the rig



f = focal ler = radius

Diverging 1

Two-Lens System Perform the calcul-Calculate the image produced by the first lens, as presence of the second. Then use the image position relative to the second lens as the object for the second calculation ignoring the first lens.

Spherical Refracting Surface This refers to two materials with a single refracting surface.

$$\frac{n_1}{p} + \frac{n_2}{i} = \frac{n_2 - n_1}{r}$$

 $M = \frac{h'}{h} = -\frac{n_1 i}{n_2 p}$

p = object distance

i = image distance [m] (positive for real images)

f = focal point [m]

n = index of refraction

r = radius [m] (positive when facing a convex surface, unlike with mirrors)

M = magnification

h' = image height [m]

h = object height [m]

Constructive and Destructive Interference by Single and Double Slit Defraction and Circular Aperture

Young's double-slit experiment (bright fringes/dark fringes):

Double Slit Constructive:

 $\Delta L = d \sin \theta = m\lambda$

Destructive:

 $\Delta L = d \sin \theta = (m + \frac{1}{2})\lambda$

d = distance between the slits [m]

 θ = the angle between a normal line extending from midway between the slits and a line extending from the midway point to the point of ray

Intensity:

 $I = I_m(\cos^2\beta) \left(\frac{\sin\alpha}{\alpha}\right)^2$

 $\beta = \frac{\pi d}{\lambda} \sin \theta$

 $\alpha = \frac{\pi a}{\lambda} \sin \theta$

Single-Slit Destructive:

 $a\sin\theta = m\lambda$

Circular Aperture st Minim

$$\sin \theta = 1$$

intersection.

m = fringe order number [integer]

 λ = wavelength of the light [m]

a = width of the single-slit [m]

 ΔL = the difference between the distance traveled of the two rays [m]

 $I = \text{intensity } \textcircled{0} \theta \ [W/m^2]$

 $I_m = \text{intensity } @ \theta = 0 [W/m^2]$

d = distance between the slits [m]

In a circular aperture, the 1st minimum is the point at which an image can no longer be

reflected ray undergoes a phase shift of 180° e reflecting material ns a greater index of n than the ambient n dium. Relative to the n than the ambient without phase shiff this constitutes a path difference

Interference beween Reflecte and Refracted rays

a thin materal stranded by another medium:

n = index of refraction

t = thickness of the material [m]

= fringe or the number [integer]

= wavelength of the light [m] ctive: $m\lambda$

bigner n and the other lower, then the above constructive destructive formulas ero eversed.

gth within a medium:

 λ = wavelength in free space [m] λ_n = wavelength in the medium [*m*] n = index of refractionc = the speed of light 3.00 × 10⁸ [m/s] $c = n\lambda_n f$

Polarizing Angle: by Brewster's Law, the angle of incidence that produces complete polarization in the reflected light from an amorphous material such as glass.

f = frequency [Hz]

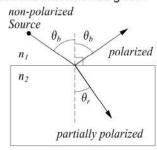
$$\tan \theta_B = \frac{n_2}{n_1}$$

$$\theta_r + \theta_B = 90^\circ$$

n = index of refraction

= angle of incidence producing 90° angle between reflected and refracted rays.

 θ_r = angle of incidence of the refracted ray.



Intensity of light passing through a polarizing lense: [Watts/m²1

initially unp initially pole $I = I_0 \cos$

